- Percent by mass =  $\frac{\text{mass of solute}}{\text{mass of solution}} \times 100$
- ppm =  $\frac{\text{mass solute}}{\text{mass solution}} \times 10^6 \text{ ppm}$
- ppb =  $\frac{\text{mass solute}}{\text{mass solution}} \times 10^9 \text{ ppb}$

# **Summary**

# 3.1 Formula Mass and the Mole Concept

The formula mass of a substance is the sum of the average atomic masses of each atom represented in the chemical formula and is expressed in atomic mass units. The formula mass of a covalent compound is also called the molecular mass. A convenient amount unit for expressing very large numbers of atoms or molecules is the mole. Experimental measurements have determined the number of entities composing 1 mole of substance to be  $6.022 \times 10^{23}$ , a quantity called Avogadro's number. The mass in grams of 1 mole of substance is its molar mass. Due to the use of the same reference substance in defining the atomic mass unit and the mole, the formula mass (amu) and molar mass (g/mol) for any substance are numerically equivalent (for example, one  $H_2O$  molecule weighs approximately 18 g).

# 3.2 Determining Empirical and Molecular Formulas

The chemical identity of a substance is defined by the types and relative numbers of atoms composing its fundamental entities (molecules in the case of covalent compounds, ions in the case of ionic compounds). A compound's percent composition provides the mass percentage of each element in the compound, and it is often experimentally determined and used to derive the compound's empirical formula. The empirical formula mass of a covalent compound may be compared to the compound's molecular or molar mass to derive a molecular formula.

# 3.3 Molarity

Solutions are homogeneous mixtures. Many solutions contain one component, called the solvent, in which other components, called solutes, are dissolved. An aqueous solution is one for which the solvent is water. The concentration of a solution is a measure of the relative amount of solute in a given amount of solution. Concentrations may be measured using various units, with one very useful unit being molarity, defined as the number of moles of solute per liter of solution. The solute concentration of a solution may be decreased by adding solvent, a process referred to as dilution. The dilution equation is a simple relation between concentrations and volumes of a solution before and after dilution.

#### 3.4 Other Units for Solution Concentrations

In addition to molarity, a number of other solution concentration units are used in various applications. Percentage concentrations based on the solution components' masses, volumes, or both are useful for expressing relatively high concentrations, whereas lower concentrations are conveniently expressed using ppm or ppb units. These units are popular in environmental, medical, and other fields where mole-based units such as molarity are not as commonly used.

### **Exercises**

#### 3.1 Formula Mass and the Mole Concept

- 1. What is the total mass (amu) of carbon in each of the following molecules?
- (a)  $CH_4$
- (b) CHCl<sub>3</sub>
- (c)  $C_{12}H_{10}O_6$
- (d) CH<sub>3</sub>CH<sub>2</sub>CH<sub>2</sub>CH<sub>2</sub>CH<sub>3</sub>

- **2.** What is the total mass of hydrogen in each of the molecules?
- (a) CH<sub>4</sub>
- (b) CHCl<sub>3</sub>
- (c)  $C_{12}H_{10}O_6$
- (d) CH<sub>3</sub>CH<sub>2</sub>CH<sub>2</sub>CH<sub>2</sub>CH<sub>3</sub>
- **3.** Calculate the molecular or formula mass of each of the following:
- (a) P<sub>4</sub>
- (b) H<sub>2</sub>O
- (c)  $Ca(NO_3)_2$
- (d) CH<sub>3</sub>CO<sub>2</sub>H (acetic acid)
- (e)  $C_{12}H_{22}O_{11}$  (sucrose, cane sugar).
- **4.** Determine the molecular mass of the following compounds:
- (a)

(b)

(c)

$$c = c$$

(d)

**5.** Determine the molecular mass of the following compounds:

(a)

$$C = C$$
 $CH_2CH_3$ 

(b)

$$H - C - C \equiv C - C - H$$

(c)

(d)

**6.** Which molecule has a molecular mass of 28.05 amu?

(a)

(b)

(c)

**7.** Write a sentence that describes how to determine the number of moles of a compound in a known mass of the compound if we know its molecular formula.

- **8.** Compare 1 mole of  $H_2$ , 1 mole of  $O_2$ , and 1 mole of  $F_2$ .
- (a) Which has the largest number of molecules? Explain why.
- (b) Which has the greatest mass? Explain why.
- **9.** Which contains the greatest mass of oxygen: 0.75 mol of ethanol ( $C_2H_5OH$ ), 0.60 mol of formic acid ( $HCO_2H$ ), or 1.0 mol of water ( $H_2O$ )? Explain why.
- **10.** Which contains the greatest number of moles of oxygen atoms: 1 mol of ethanol ( $C_2H_5OH$ ), 1 mol of formic acid ( $HCO_2H$ ), or 1 mol of water ( $H_2O$ )? Explain why.
- 11. How are the molecular mass and the molar mass of a compound similar and how are they different?
- **12.** Calculate the molar mass of each of the following compounds:
- (a) hydrogen fluoride, HF
- (b) ammonia, NH<sub>3</sub>
- (c) nitric acid, HNO<sub>3</sub>
- (d) silver sulfate, Ag<sub>2</sub>SO<sub>4</sub>
- (e) boric acid, B(OH)<sub>3</sub>
- **13.** Calculate the molar mass of each of the following:
- (a)  $S_8$
- (b)  $C_5H_{12}$
- (c)  $Sc_2(SO_4)_3$
- (d) CH<sub>3</sub>COCH<sub>3</sub> (acetone)
- (e)  $C_6H_{12}O_6$  (glucose)
- **14.** Calculate the empirical or molecular formula mass and the molar mass of each of the following minerals:
- (a) limestone, CaCO<sub>3</sub>
- (b) halite, NaCl
- (c) beryl, Be<sub>3</sub>Al<sub>2</sub>Si<sub>6</sub>O<sub>18</sub>
- (d) malachite, Cu<sub>2</sub>(OH)<sub>2</sub>CO<sub>3</sub>
- (e) turquoise, CuAl<sub>6</sub>(PO<sub>4</sub>)<sub>4</sub>(OH)<sub>8</sub>(H<sub>2</sub>O)<sub>4</sub>
- **15.** Calculate the molar mass of each of the following:
- (a) the anesthetic halothane, C<sub>2</sub>HBrClF<sub>3</sub>
- (b) the herbicide paraquat, C<sub>12</sub>H<sub>14</sub>N<sub>2</sub>Cl<sub>2</sub>
- (c) caffeine,  $C_8H_{10}N_4O_2$
- (d) urea,  $CO(NH_2)_2$
- (e) a typical soap, C<sub>17</sub>H<sub>35</sub>CO<sub>2</sub>Na
- **16.** Determine the number of moles of compound and the number of moles of each type of atom in each of the following:
- (a) 25.0 g of propylene,  $C_3H_6$
- (b)  $3.06 \times 10^{-3}$  g of the amino acid glycine,  $C_2H_5NO_2$
- (c) 25 lb of the herbicide Treflan,  $C_{13}H_{16}N_2O_4F$  (1 lb = 454 g)
- (d) 0.125 kg of the insecticide Paris Green, Cu<sub>4</sub>(AsO<sub>3</sub>)<sub>2</sub>(CH<sub>3</sub>CO<sub>2</sub>)<sub>2</sub>
- (e) 325 mg of aspirin,  $C_6H_4(CO_2H)(CO_2CH_3)$

- **17.** Determine the mass of each of the following:
- (a) 0.0146 mol KOH
- (b) 10.2 mol ethane,  $C_2H_6$
- (c)  $1.6 \times 10^{-3} \text{ mol Na}_2 \text{ SO}_4$
- (d)  $6.854 \times 10^3$  mol glucose,  $C_6 H_{12} O_6$
- (e) 2.86 mol Co(NH<sub>3</sub>)<sub>6</sub>Cl<sub>3</sub>
- **18.** Determine the number of moles of the compound and determine the number of moles of each type of atom in each of the following:
- (a) 2.12 g of potassium bromide, KBr
- (b) 0.1488 g of phosphoric acid, H<sub>3</sub>PO<sub>4</sub>
- (c) 23 kg of calcium carbonate, CaCO<sub>3</sub>
- (d) 78.452 g of aluminum sulfate, Al<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub>
- (e) 0.1250 mg of caffeine,  $C_8H_{10}N_4O_2$
- **19.** Determine the mass of each of the following:
- (a) 2.345 mol LiCl
- (b) 0.0872 mol acetylene, C<sub>2</sub>H<sub>2</sub>
- (c)  $3.3 \times 10^{-2} \text{ mol Na}_2 \text{ CO}_3$
- (d)  $1.23 \times 10^3$  mol fructose,  $C_6 H_{12} O_6$
- (e) 0.5758 mol FeSO<sub>4</sub>(H<sub>2</sub>O)<sub>7</sub>
- **20.** The approximate minimum daily dietary requirement of the amino acid leucine,  $C_6H_{13}NO_2$ , is 1.1 g. What is this requirement in moles?
- **21.** Determine the mass in grams of each of the following:
- (a) 0.600 mol of oxygen atoms
- (b) 0.600 mol of oxygen molecules, O2
- (c) 0.600 mol of ozone molecules,  $O_3$
- **22.** A 55-kg woman has  $7.5 \times 10^{-3}$  mol of hemoglobin (molar mass = 64,456 g/mol) in her blood. How many hemoglobin molecules is this? What is this quantity in grams?
- **23.** Determine the number of atoms and the mass of zirconium, silicon, and oxygen found in 0.3384 mol of zircon,  $ZrSiO_4$ , a semiprecious stone.
- **24.** Determine which of the following contains the greatest mass of hydrogen: 1 mol of  $CH_4$ , 0.6 mol of  $C_6H_6$ , or 0.4 mol of  $C_3H_8$ .
- **25.** Determine which of the following contains the greatest mass of aluminum: 122 g of AlPO<sub>4</sub>, 266 g of Al<sub>2</sub>C1<sub>6</sub>, or 225 g of Al<sub>2</sub>S<sub>3</sub>.
- **26.** Diamond is one form of elemental carbon. An engagement ring contains a diamond weighing 1.25 carats (1 carat = 200 mg). How many atoms are present in the diamond?
- **27.** The Cullinan diamond was the largest natural diamond ever found (January 25, 1905). It weighed 3104 carats (1 carat = 200 mg). How many carbon atoms were present in the stone?
- **28.** One 55-gram serving of a particular cereal supplies 270 mg of sodium, 11% of the recommended daily allowance. How many moles and atoms of sodium are in the recommended daily allowance?
- **29.** A certain nut crunch cereal contains 11.0 grams of sugar (sucrose,  $C_{12}H_{22}O_{11}$ ) per serving size of 60.0 grams. How many servings of this cereal must be eaten to consume 0.0278 moles of sugar?

- **30.** A tube of toothpaste contains 0.76 g of sodium monofluorophosphate (Na<sub>2</sub>PO<sub>3</sub>F) in 100 mL.
- (a) What mass of fluorine atoms in mg was present?
- (b) How many fluorine atoms were present?
- **31.** Which of the following represents the least number of molecules?
- (a) 20.0 g of  $H_2O$  (18.02 g/mol)
- (b) 77.0 g of CH<sub>4</sub> (16.06 g/mol)
- (c) 68.0 g of CaH<sub>2</sub> (42.09 g/mol)
- (d) 100.0 g of N<sub>2</sub>O (44.02 g/mol)
- (e) 84.0 g of HF (20.01 g/mol)

# 3.2 Determining Empirical and Molecular Formulas

- **32.** What information do we need to determine the molecular formula of a compound from the empirical formula?
- **33.** Calculate the following to four significant figures:
- (a) the percent composition of ammonia, NH<sub>3</sub>
- (b) the percent composition of photographic fixer solution ("hypo"), Na<sub>2</sub>S<sub>2</sub>O<sub>3</sub>
- (c) the percent of calcium ion in Ca<sub>3</sub>(PO<sub>4</sub>)<sub>2</sub>
- **34.** Determine the following to four significant figures:
- (a) the percent composition of hydrazoic acid, HN<sub>3</sub>
- (b) the percent composition of TNT, C<sub>6</sub>H<sub>2</sub>(CH<sub>3</sub>)(NO<sub>2</sub>)<sub>3</sub>
- (c) the percent of  $SO_4^{2-}$  in  $Al_2(SO_4)_3$
- **35.** Determine the percent ammonia, NH<sub>3</sub>, in Co(NH<sub>3</sub>)<sub>6</sub>Cl<sub>3</sub>, to three significant figures.
- **36.** Determine the percent water in CuSO<sub>4</sub>·5H<sub>2</sub>O to three significant figures.
- **37.** Determine the empirical formulas for compounds with the following percent compositions:
- (a) 15.8% carbon and 84.2% sulfur
- (b) 40.0% carbon, 6.7% hydrogen, and 53.3% oxygen
- **38.** Determine the empirical formulas for compounds with the following percent compositions:
- (a) 43.6% phosphorus and 56.4% oxygen
- (b) 28.7% K, 1.5% H, 22.8% P, and 47.0% O
- **39.** A compound of carbon and hydrogen contains 92.3% C and has a molar mass of 78.1 g/mol. What is its molecular formula?
- **40.** Dichloroethane, a compound that is often used for dry cleaning, contains carbon, hydrogen, and chlorine. It has a molar mass of 99 g/mol. Analysis of a sample shows that it contains 24.3% carbon and 4.1% hydrogen. What is its molecular formula?
- **41.** Determine the empirical and molecular formula for chrysotile asbestos. Chrysotile has the following percent composition: 28.03% Mg, 21.60% Si, 1.16% H, and 49.21% O. The molar mass for chrysotile is 520.8 g/mol.

- **42.** Polymers are large molecules composed of simple units repeated many times. Thus, they often have relatively simple empirical formulas. Calculate the empirical formulas of the following polymers:
- (a) Lucite (Plexiglas); 59.9% C, 8.06% H, 32.0% O
- (b) Saran; 24.8% C, 2.0% H, 73.1% Cl
- (c) polyethylene; 86% C, 14% H
- (d) polystyrene; 92.3% C, 7.7% H
- (e) Orlon; 67.9% C, 5.70% H, 26.4% N
- **43.** A major textile dye manufacturer developed a new yellow dye. The dye has a percent composition of 75.95% C, 17.72% N, and 6.33% H by mass with a molar mass of about 240 g/mol. Determine the molecular formula of the dye.

# 3.3 Molarity

- **44.** Explain what changes and what stays the same when 1.00 L of a solution of NaCl is diluted to 1.80 L.
- **45.** What information do we need to calculate the molarity of a sulfuric acid solution?
- **46.** What does it mean when we say that a 200-mL sample and a 400-mL sample of a solution of salt have the same molarity? In what ways are the two samples identical? In what ways are these two samples different?
- **47.** Determine the molarity for each of the following solutions:
- (a) 0.444 mol of CoCl<sub>2</sub> in 0.654 L of solution
- (b) 98.0 g of phosphoric acid, H<sub>3</sub>PO<sub>4</sub>, in 1.00 L of solution
- (c) 0.2074 g of calcium hydroxide, Ca(OH)<sub>2</sub>, in 40.00 mL of solution
- (d) 10.5 kg of Na<sub>2</sub>SO<sub>4</sub>·10H<sub>2</sub>O in 18.60 L of solution
- (e)  $7.0 \times 10^{-3}$  mol of  $I_2$  in 100.0 mL of solution
- (f)  $1.8 \times 10^4$  mg of HCl in 0.075 L of solution
- **48.** Determine the molarity of each of the following solutions:
- (a) 1.457 mol KCl in 1.500 L of solution
- (b) 0.515 g of  $H_2SO_4$  in 1.00 L of solution
- (c) 20.54 g of Al(NO<sub>3</sub>)<sub>3</sub> in 1575 mL of solution
- (d) 2.76 kg of  $CuSO_4 \cdot 5H_2O$  in 1.45 L of solution
- (e) 0.005653 mol of Br<sub>2</sub> in 10.00 mL of solution
- (f) 0.000889 g of glycine, C<sub>2</sub>H<sub>5</sub>NO<sub>2</sub>, in 1.05 mL of solution
- **49.** Consider this question: What is the mass of the solute in 0.500 L of 0.30 M glucose,  $C_6H_{12}O_6$ , used for intravenous injection?
- (a) Outline the steps necessary to answer the question.
- (b) Answer the question.
- **50.** Consider this question: What is the mass of solute in 200.0 L of a 1.556-*M* solution of KBr?
- (a) Outline the steps necessary to answer the question.
- (b) Answer the question.

- **51.** Calculate the number of moles and the mass of the solute in each of the following solutions:
- (a) 2.00 L of 18.5 M H<sub>2</sub>SO<sub>4</sub>, concentrated sulfuric acid
- (b) 100.0 mL of 3.8  $\times$  10<sup>-5</sup> *M* NaCN, the minimum lethal concentration of sodium cyanide in blood serum
- (c) 5.50 L of 13.3 M H<sub>2</sub>CO, the formaldehyde used to "fix" tissue samples
- (d) 325 mL of 1.8  $\times$  10<sup>-6</sup> M FeSO<sub>4</sub>, the minimum concentration of iron sulfate detectable by taste in drinking water
- **52.** Calculate the number of moles and the mass of the solute in each of the following solutions:
- (a) 325 mL of 8.23  $\times$  10<sup>-5</sup> *M* KI, a source of iodine in the diet
- (b) 75.0 mL of 2.2  $\times$  10<sup>-5</sup> M H<sub>2</sub>SO<sub>4</sub>, a sample of acid rain
- (c) 0.2500 L of 0.1135 M K<sub>2</sub>CrO<sub>4</sub>, an analytical reagent used in iron assays
- (d) 10.5 L of 3.716 M (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub>, a liquid fertilizer
- **53.** Consider this question: What is the molarity of  $KMnO_4$  in a solution of 0.0908 g of  $KMnO_4$  in 0.500 L of solution?
- (a) Outline the steps necessary to answer the question.
- (b) Answer the question.
- **54.** Consider this question: What is the molarity of HCl if 35.23 mL of a solution of HCl contain 0.3366 g of HCl?
- (a) Outline the steps necessary to answer the question.
- (b) Answer the question.
- **55.** Calculate the molarity of each of the following solutions:
- (a) 0.195 g of cholesterol, C<sub>27</sub>H<sub>46</sub>O, in 0.100 L of serum, the average concentration of cholesterol in human serum
- (b) 4.25 g of NH<sub>3</sub> in 0.500 L of solution, the concentration of NH<sub>3</sub> in household ammonia
- (c) 1.49 kg of isopropyl alcohol,  $C_3H_7OH$ , in 2.50 L of solution, the concentration of isopropyl alcohol in rubbing alcohol
- (d) 0.029 g of  $I_2$  in 0.100 L of solution, the solubility of  $I_2$  in water at 20 °C
- **56.** Calculate the molarity of each of the following solutions:
- (a) 293 g HCl in 666 mL of solution, a concentrated HCl solution
- (b) 2.026 g FeCl<sub>3</sub> in 0.1250 L of a solution used as an unknown in general chemistry laboratories
- (c) 0.001 mg Cd<sup>2+</sup> in 0.100 L, the maximum permissible concentration of cadmium in drinking water
- (d) 0.0079 g C<sub>7</sub>H<sub>5</sub>SNO<sub>3</sub> in one ounce (29.6 mL), the concentration of saccharin in a diet soft drink.
- **57.** There is about 1.0 g of calcium, as Ca<sup>2+</sup>, in 1.0 L of milk. What is the molarity of Ca<sup>2+</sup> in milk?
- **58.** What volume of a 1.00-*M* Fe(NO<sub>3</sub>)<sub>3</sub> solution can be diluted to prepare 1.00 L of a solution with a concentration of 0.250 *M*?
- **59.** If 0.1718 L of a  $0.3556\text{-}M \text{ C}_3\text{H}_7\text{OH}$  solution is diluted to a concentration of 0.1222 M, what is the volume of the resulting solution?
- **60.** If 4.12 L of a  $0.850 \text{ }M\text{-H}_3\text{PO}_4$  solution is be diluted to a volume of 10.00 L, what is the concentration of the resulting solution?
- **61.** What volume of a 0.33-M  $C_{12}H_{22}O_{11}$  solution can be diluted to prepare 25 mL of a solution with a concentration of 0.025 M?
- **62.** What is the concentration of the NaCl solution that results when 0.150 L of a 0.556-*M* solution is allowed to evaporate until the volume is reduced to 0.105 L?

- **63.** What is the molarity of the diluted solution when each of the following solutions is diluted to the given final volume?
- (a) 1.00 L of a 0.250-M solution of Fe(NO<sub>3</sub>)<sub>3</sub> is diluted to a final volume of 2.00 L
- (b) 0.5000 L of a 0.1222-M solution of  $C_3H_7OH$  is diluted to a final volume of 1.250 L
- (c) 2.35 L of a 0.350-M solution of H<sub>3</sub>PO<sub>4</sub> is diluted to a final volume of 4.00 L
- (d) 22.50 mL of a 0.025-M solution of  $C_{12}H_{22}O_{11}$  is diluted to 100.0 mL
- **64.** What is the final concentration of the solution produced when 225.5 mL of a 0.09988-*M* solution of Na<sub>2</sub>CO<sub>3</sub> is allowed to evaporate until the solution volume is reduced to 45.00 mL?
- **65.** A 2.00-L bottle of a solution of concentrated HCl was purchased for the general chemistry laboratory. The solution contained 868.8 g of HCl. What is the molarity of the solution?
- **66.** An experiment in a general chemistry laboratory calls for a 2.00-*M* solution of HCl. How many mL of 11.9 *M* HCl would be required to make 250 mL of 2.00 *M* HCl?
- **67.** What volume of a 0.20- $M K_2 SO_4$  solution contains 57 g of  $K_2 SO_4$ ?
- **68.** The US Environmental Protection Agency (EPA) places limits on the quantities of toxic substances that may be discharged into the sewer system. Limits have been established for a variety of substances, including hexavalent chromium, which is limited to 0.50 mg/L. If an industry is discharging hexavalent chromium as potassium dichromate ( $K_2Cr_2O_7$ ), what is the maximum permissible molarity of that substance?

# 3.4 Other Units for Solution Concentrations

- **69.** Consider this question: What mass of a concentrated solution of nitric acid (68.0% HNO<sub>3</sub> by mass) is needed to prepare 400.0 g of a 10.0% solution of HNO<sub>3</sub> by mass?
- (a) Outline the steps necessary to answer the question.
- (b) Answer the question.
- **70.** What mass of a 4.00% NaOH solution by mass contains 15.0 g of NaOH?
- **71.** What mass of solid NaOH (97.0% NaOH by mass) is required to prepare 1.00 L of a 10.0% solution of NaOH by mass? The density of the 10.0% solution is 1.109 g/mL.
- **72.** What mass of HCl is contained in 45.0 mL of an aqueous HCl solution that has a density of  $1.19 \text{ g cm}^{-3}$  and contains 37.21% HCl by mass?
- **73.** The hardness of water (hardness count) is usually expressed in parts per million (by mass) of  $CaCO_3$ , which is equivalent to milligrams of  $CaCO_3$  per liter of water. What is the molar concentration of  $Ca^{2+}$  ions in a water sample with a hardness count of 175 mg  $CaCO_3/L$ ?
- **74.** The level of mercury in a stream was suspected to be above the minimum considered safe (1 part per billion by weight). An analysis indicated that the concentration was 0.68 parts per billion. Assume a density of 1.0 g/mL and calculate the molarity of mercury in the stream.
- **75.** In Canada and the United Kingdom, devices that measure blood glucose levels provide a reading in millimoles per liter. If a measurement of 5.3 mM is observed, what is the concentration of glucose ( $C_6H_{12}O_6$ ) in mg/dL?
- **76.** A throat spray is 1.40% by mass phenol,  $C_6H_5OH$ , in water. If the solution has a density of 0.9956 g/mL, calculate the molarity of the solution.
- **77.** Copper(I) iodide (CuI) is often added to table salt as a dietary source of iodine. How many moles of CuI are contained in 1.00 lb (454 g) of table salt containing 0.0100% CuI by mass?
- **78.** A cough syrup contains 5.0% ethyl alcohol,  $C_2H_5OH$ , by mass. If the density of the solution is 0.9928 g/mL, determine the molarity of the alcohol in the cough syrup.
- **79.** D5W is a solution used as an intravenous fluid. It is a 5.0% by mass solution of dextrose ( $C_6H_{12}O_6$ ) in water. If the density of D5W is 1.029 g/mL, calculate the molarity of dextrose in the solution.
- **80.** Find the molarity of a 40.0% by mass aqueous solution of sulfuric acid, H<sub>2</sub>SO<sub>4</sub>, for which the density is 1.3057 g/mL.